

# Multiple imputation to handle missing covariate data in pharmacometrics modelling

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# Missing covariate data

- Common issue in pharmacometrics
- Various missing mechanisms
- Proper handling of missing covariate is crucial!



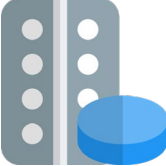
# Handling missing covariate data in pharmacometrics


- **Single imputation (SI)** >>> high risk of bias 
- **Multiple imputation (MI)** >>> preferred but underexplored 
- No published study compared SI and MI under various degrees of missing covariate data 

**Aim: Compare the accuracy of SI and MI for handling different levels of covariate missingness in pharmacometrics modeling**

# Data source<sup>1</sup>

- Complete dataset 

- Oral warfarin – single dose – 32 healthy volunteers 

- 251 warfarin concentrations – median of 6 per subject 

- Sampling times:  $t = \{0.25, 0.5, 1.0, 2.0, 4.0, 6.0, 12.0, 24.0, 48.0, 72.0, 96.0\}$  hours after dose 

- Patient characteristics: body weight, sex and age 

# Structural popPK model

- A one-compartment model >>>  $K_a$ ,  $V_d$  and  $CL$
- Inter-individual variability >>>  $K_a$ ,  $V_d$  and  $CL$
- Residual variability >>> combined additive and proportional
- Covariate model:

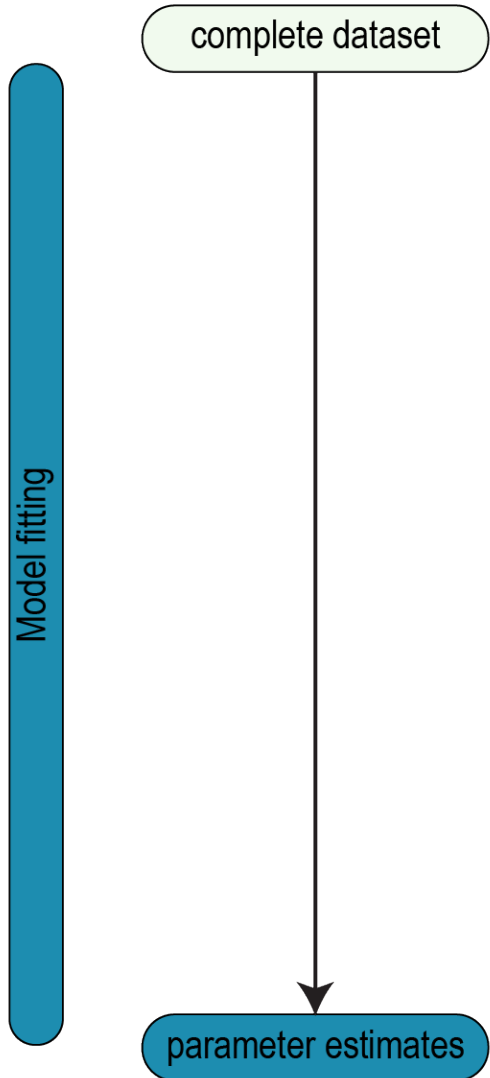
$$TVCL = \theta_{1-CL} \times \left( \frac{WT}{WT_{\text{median}}} \right)^{\theta_{2-CL}}$$

$$TVVd = \theta_{1-Vd} \times \left( \frac{WT}{WT_{\text{median}}} \right)^{\theta_{2-Vd}}$$

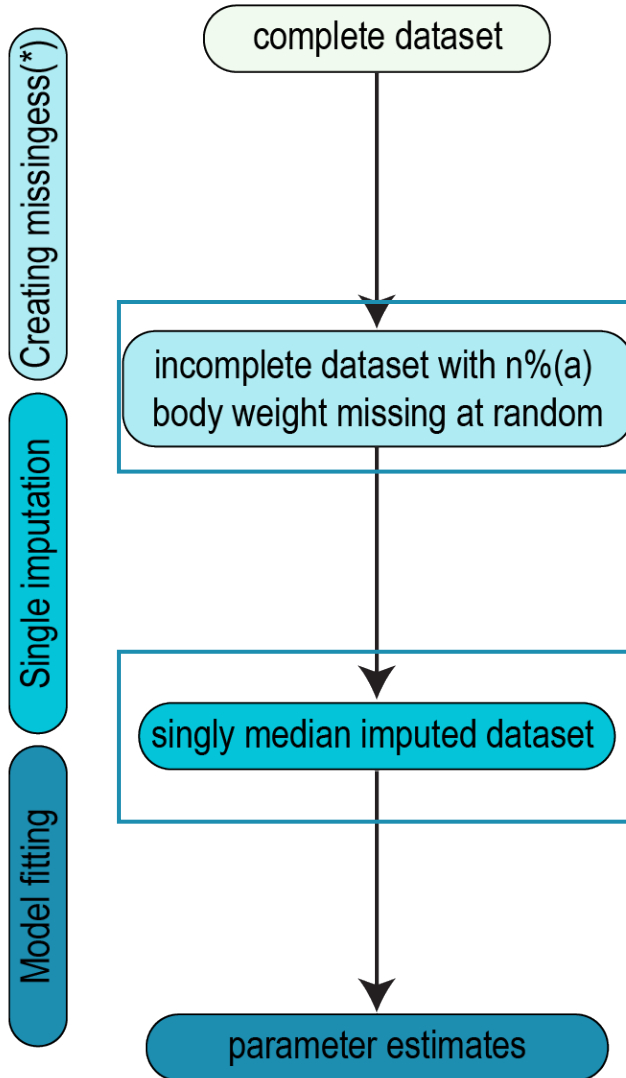


# Case study workflow

Complete dataset analysis

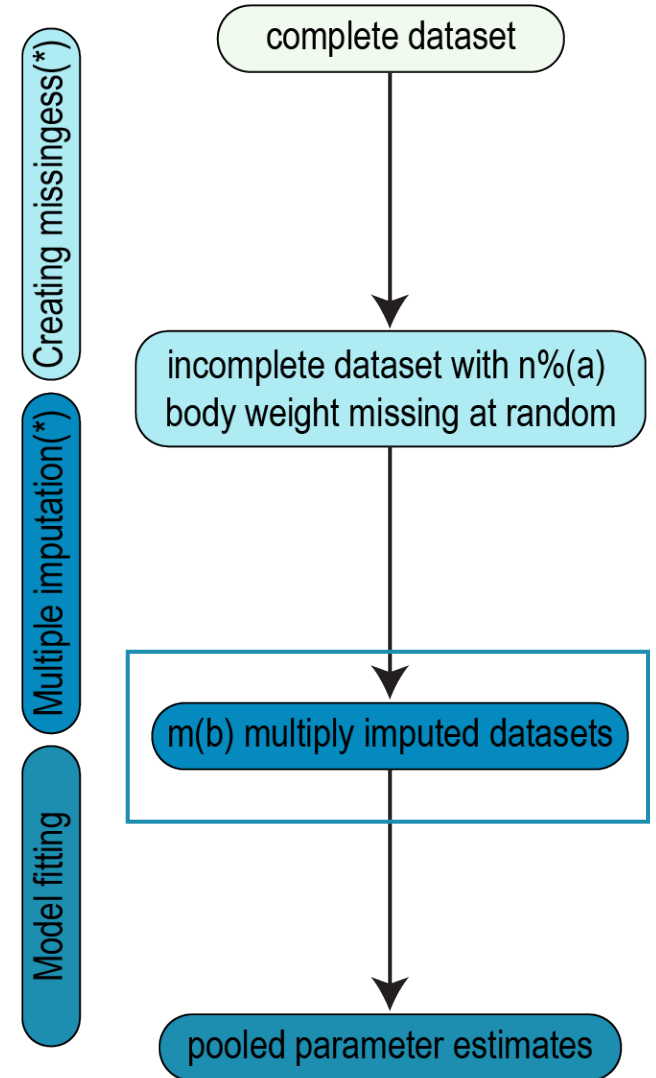


Singly imputed datasets analysis



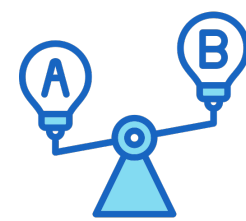
(a)  $n \in \{6.25, 12.5, 25, 50, 75\}$  (\*) repeated 30 times

Multiply imputed datasets analysis



(a)  $n \in \{6.25, 12.5, 25, 50, 75\}$  (\*) repeated 30 times  
(b)  $m \in \{20, 30, 45, 70, 105\}$

# Performance assessment – SI and MI



- Model stability >>> model convergence rate

- Accuracy in estimating point estimates:

- $$|\text{rBias\_estimate}(\%)| = \left| \frac{\text{CovariateEstimate}_{\text{SI/MI}} - \text{CovariateEstimate}_{\text{complete}}}{\text{CovariateEstimate}_{\text{complete}}} \right| \times 100\%$$

- Compared  $|\text{rBias\_estimate}(\%)|$  >>> Wilcoxon rank-sum test

- Accuracy in reflecting uncertainty estimates:

- $$|\text{rBias\_standard-error}(\%)| = \left| \frac{\text{Standard-Error}_{\text{SI/MI}} - \text{Standard-Error}_{\text{complete}}}{\text{Standard-Error}_{\text{complete}}} \right| \times 100\%$$

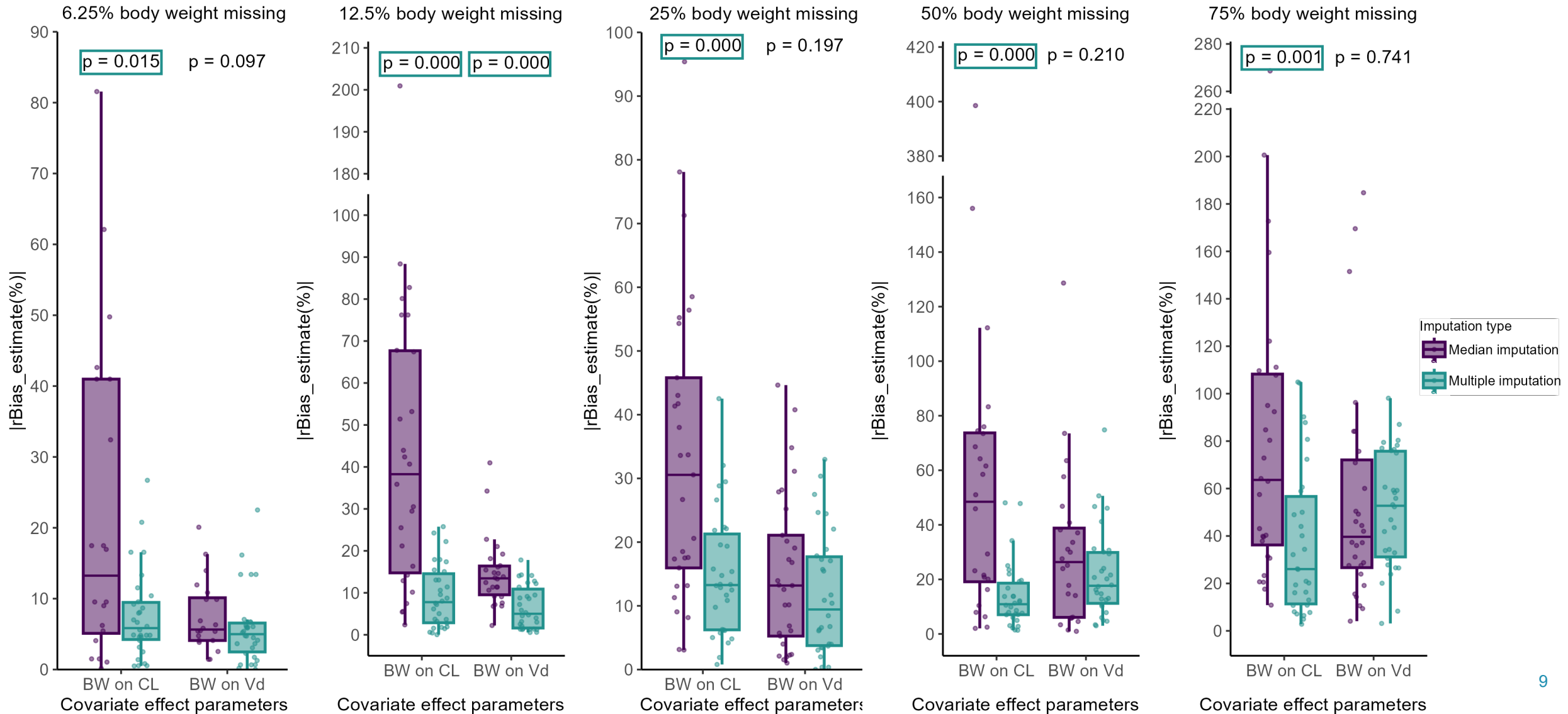
- Compared  $|\text{rBias\_standard-error}(\%)|$  >>> Wilcoxon rank-sum test

- Compared variances of  $|\text{rBias\_standard-error}(\%)|$  >>> Fligner-Killeen test

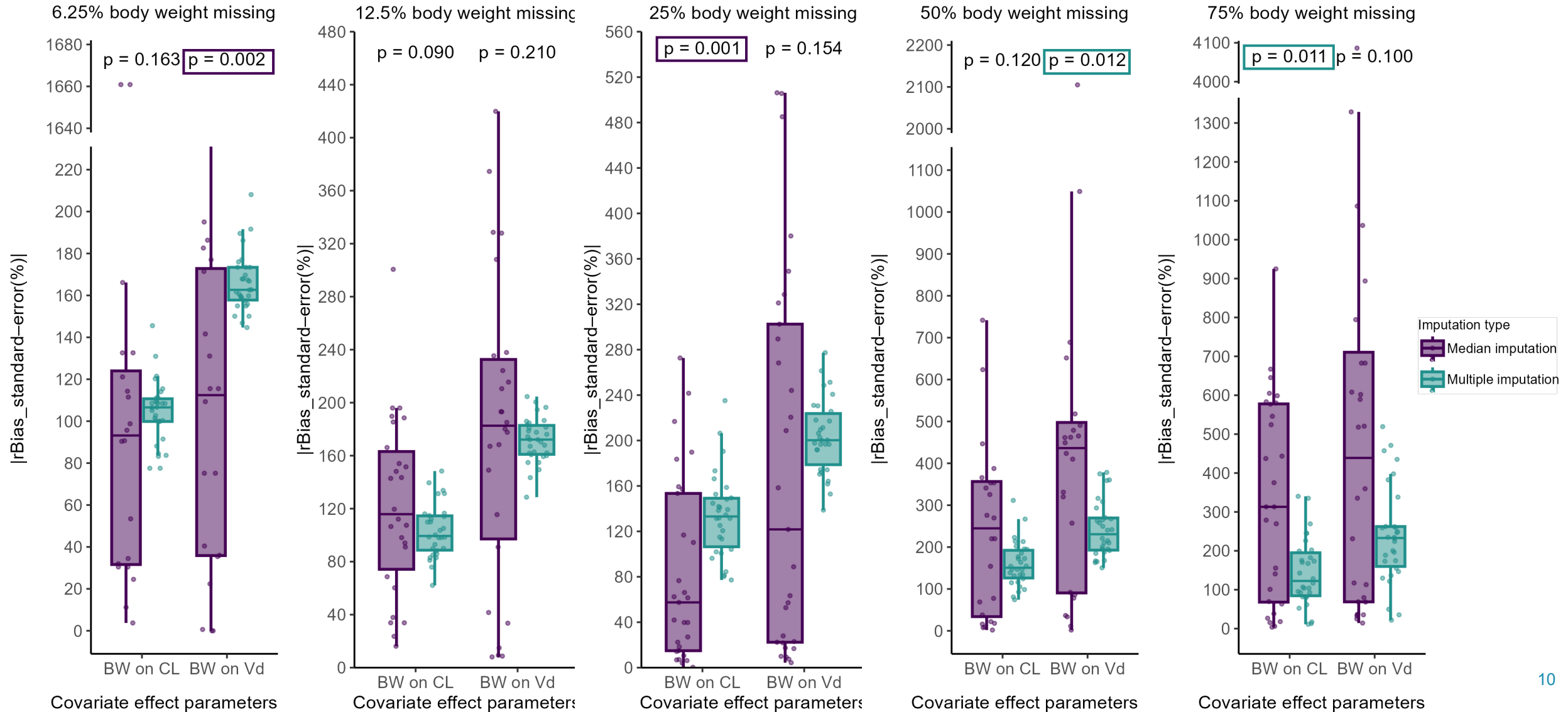
# Model convergence rate is stable across 5 scenarios

|                            |  | 6.25% BW                      | 12.5% BW                      | 25% BW                        | 50% BW                       | 75% BW                       |
|----------------------------|--|-------------------------------|-------------------------------|-------------------------------|------------------------------|------------------------------|
| Missingness scenario       |  | missing                       | missing                       | missing                       | missing                      | missing                      |
| <b>Single imputation</b>   | Number of imputation                                   | 30                            | 30                            | 30                            | 30                           | 30                           |
|                            | Number of converged models (%)                         | 20 (66.7)                     | 26 (86.7)                     | 29 (96.7)                     | 24 (80.0)                    | 28 (93.3)                    |
| <b>Multiple imputation</b> | Number of imputations                                  | 20                            | 30                            | 45                            | 70                           | 105                          |
|                            | Number of converged models<br>(median [min – max])     | 17 (11 – 20)                  | 26 (19 – 30)                  | 38 (29 – 45)                  | 62 (50 – 69)                 | 95 (75 – 103)                |
|                            | Percentage of converged models<br>(median [min – max]) | <b>85.0</b><br>(55.0 – 100.0) | <b>86.7</b><br>(63.3 – 100.0) | <b>84.4</b><br>(64.4 – 100.0) | <b>88.6</b><br>(71.4 – 98.6) | <b>90.5</b><br>(71.4 – 98.1) |

# Multiple imputation yielded significantly more accurate covariate effect estimates



# Multiple imputation produced more reliable uncertainty estimate at higher missing rates



# Conclusions

- MI provides **more accurate** covariate effect **estimates** and **better uncertainty reflection**.



- We encourage **pharmacometricians** to **adopt MI over SI**



- **Get started:** mice, mimp





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